

# Modelling the “Animal Spirits” of bank’s lending behaviour

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## Passive Intermediary vs. Active Credit Creator

- In the traditional banking literature that attempts to address this real-financial interaction problem, the commercial bank is often modelled as a passive intermediary that channel funds from the ultimate borrower to the ultimate lender (Allen and Gale 2000; Bernanke et al, 1999; Fama, 1980).
  - In reality however, the role of banks goes beyond a passive intermediary that channels funds from lenders to borrowers.
  - In the presence of fractional banking system, it functions as an active credit creator.
- In other words, the banks behaviour is not a passive reflection of the conditions of the economy, but is in itself an important factor that influences the economy via credit creation.

## Bank’s Lending Attitude

- Another important aspect, which is overlooked in the traditional banking literature, is the role of banks lending attitude (Asanuma, 2012).
  - An optimistic attitude in the banking sector collectively lowers the lending standard and prompt banks to collectively over-lend to a particular sector such as real estate.
  - It potentially leads to the development of a credit bubble.
  - A collectively pessimistic banking system not only hinders economic growth but also renders expansionary monetary policy ineffective.
- In the aftermath of the crisis, the money base has tripled due to three rounds of Quantitative Easing (QE).
- It has virtually no effect on the growth of broad money due to an inactive and pessimistic banking sector (Koo, 2011).

# The Money Base and M2

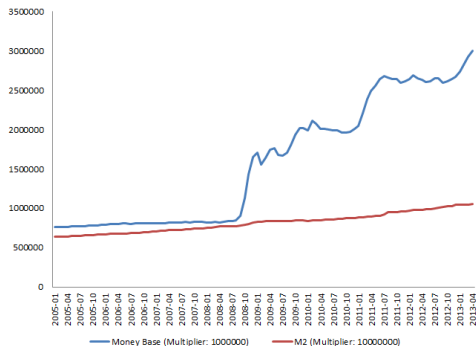


Figure 1: The Effect of Quantitative Easing on Money Base and M2<sup>1</sup>

<sup>1</sup>Source: the Federal Reserve Data Release H.3 (Aggregate Reserves of Depository Institutions and the Monetary Base) and H.6 (Money Stock Measures)

# Keynes’ “Animal Spirit” Argument

- Keynes (1936)
  - *most, probably, of our decisions to do something positive, the full consequences of which will be drawn out over many days to come, can only be taken as a result of **animal spirits**: of a spontaneous urge to action rather than inaction, and not as the outcome of a weighted average of quantitative benefits multiplied by quantitative probabilities.*
- Two important characteristics of the animal spirit.
  - Self-reinforcing: an optimistic/pessimistic sentiment will bring forth a positive/negative outcome to the market, which further reinforces the optimistic/pessimistic sentiment.
  - Contagion: sentiment spreads and it eventually leads to herding amongst agents.
- Empirical evidence on herding in financial markets and financial institutions: (Bikhchandani and Sharma 2000; Haiss, 2005; Nagawaka and Uchida, 2007; Liu, 2012).

# Literature Review

- Current Literature that models the "animal spirit"
  - Lux (1995) proposes a seminal work that examines the relationship between investors sentiment, asset price bubble and crash by applying the stochastic aggregation method;
  - Franke (2010) applies the Lux model in the context of macroeconomic dynamics. He studies the interplay between the firm's sentiment, inflation climate, and the interest rate;
  - Charpe et al (2012) further extends Franke (2010) and proposes a Dynamic Stochastic General Disequilibrium (DSGD) Model of Real-Financial interaction;
  - De Grauwe (2010) develops a DSGE model that is augmented by agents cognitive limitations;
  - Asanuma (2012) examines how banks lending attitude affects economic growth in an agent-based setting.

# Objective of the paper

- This paper examines the role of “animal spirits”, here represented as, in determining banks’ lending behaviour.
- The aim is to assess how the contagious waves of optimism and pessimism contributes to the boom-bust of the credit cycle.
  - It is via a modification of the bank’s balance sheet positions, and how it amplifies the business cycle in the real sector.
- Main Contributions
  - To the best of our knowledge, this paper represents the first attempt to model the banking behaviour as influenced by animal spirits.
  - We introduce the heterogeneity in the credit sector, which represent a novelty in this stream of aggregative dynamical model.
  - We stress the role of the mechanism of credit-creation by banks as a potentially destabilising factor.

# The Balance Sheet of a Typical Commercial Bank

Asset	Liability
<b>R (Reserve)</b>	D (Deposit)
<b>L (Loan)</b>	CB (Central Bank Borrowing)
B (Bond)	IB (Interbank Borrowing)
	E (Bank Equity)

Table 1: A Simplified Balance Sheet of Commercial Bank

- Following Taylor (2004), we focus on the loan-to-reserve ratio ( $\lambda^s$ )

$$L^s = \lambda^s T_c, \quad (1)$$

- Here  $L^s$  is the level of aggregate credit supply,  $\lambda^s$  is the loan-to-reserve ratio of banks, and  $T_c$  is the level of unborrowed reserves.
- The  $\lambda^s$  reflects not only bank's lending attitude, but also the amount of debt accumulation due to banks' loan creation.



## The average opinion index $x$

- We consider the following baseline model, where we categorize banks into two groups, i.e. the optimistic banks and the pessimistic banks.
- Formally, suppose that there are  $2N$  banks in the economy, of which  $n_+$  is the number of optimists and  $n_-$  are the number of pessimists, thus  $n_+ + n_- = 2N$ .
- Following Lux (1995), we focus on the difference in the size of the two groups by defining the index  $x$ , where

$$x = (n_+ - n_-)/2N. \quad (2)$$

## The aggregate availability of credit $L^s$

- Recall that  $L^s = \lambda^s T_c$ ,  $T_c = 2NR$ .
- Given that there are two groups of banks in our model, and each group has different loan-to-reserve ratios. We modify the equation to

$$L^s = R(n_+ \lambda_+ + n_- \lambda_-). \quad (3)$$

- In the baseline model, we assume that the optimistic banks are active and the pessimistic banks are inactive ( $\lambda_- = 0$ ). We have

$$L^s = Rn_+ \lambda_+ = RN(1+x)\lambda_+ = (T_c/2)(1+x)\lambda_+. \quad (4)$$

## The dynamics of the average opinion index $x$

- We follow Lux (1995) to model the average opinion  $x$ . The change in  $x$  depends on the size of each group multiplied by their transition probability:

$$\dot{x} = (1 - x)p_{+-} - (1 + x)p_{-+}. \quad (5)$$

- Here  $p_{+-}$  is the transition probability that a pessimistic bank becomes an optimistic one, and likewise for  $p_{-+}$ .
- The Opinion Formation Index:

$$s(x, \lambda_+, d) = a_1 x + a_2 \lambda_+ + a_3 (y^d - y) + d. \quad (6)$$

- Here  $a_1, a_2, a_3$  are three cognitive parameters;  $d$  is a general financial condition index.
- The Switching Probability:

$$p_{+-} = v \cdot \exp(s), \quad (7)$$

$$p_{-+} = v \cdot \exp(-s). \quad (8)$$

- Hence:

$$\dot{x} = v[(1 - x) \exp(s) - (1 + x) \exp(-s)]. \quad (9)$$

## The dynamics of $\lambda_+$

- We assume that the optimistic banks make decisions based on the average opinion  $x$ , as well as development in the real sector  $\dot{y}$ .
- The law of motion for  $\lambda_+$  can be formulated as

$$\dot{\lambda}_+ = \gamma_1 x + \gamma_2 \dot{y}. \quad (10)$$

- Here  $\gamma_1$  and  $\gamma_2$  are two action parameters,  $\gamma_1$  is the speed of adjustment toward the average opinion and  $\gamma_2$  is the speed of adjustment toward the change in output ( $\dot{y}$ ).

## The dynamic multiplier of output

- Following Blanchard (1981), we assume that output moves according to a standard dynamic multiplier process,
  - except that the availability of credit  $L^s$  determines the aggregate demand ( $y^d$ ):

$$\dot{y} = \sigma(y^d - y), \quad (11)$$

$$y^d = y_0^d + kL^s, \quad (12)$$

$$L^s = (T_c/2)(1+x)\lambda_+. \quad (13)$$

- Here  $y$  is the output;  $y^d$  is the aggregate demand;  $y_0^d$  is the autonomous component of the aggregate demand.
  - Hence

$$\dot{y} = \sigma(y_0^d + k(T_c/2)(1+x)\lambda_+ - y). \quad (14)$$

## The 3D Baseline Model

- Given the above assumptions, the 3D system with a real sector becomes

$$\dot{\lambda}_+ = \gamma_1 x + \gamma_2 \dot{y}, \quad (15)$$

$$\dot{y} = \sigma(y_0^d + k(T_c/2)(1+x)\lambda_+ - y), \quad (16)$$

$$\dot{x} = v[(1-x)\exp(s(\cdot)) - (1+x)\exp(-s(\cdot))]. \quad (17)$$

- Here  $s(\cdot) = a_1 x + a_2 \lambda_+ + a_3 (y^d - y) + d$ .

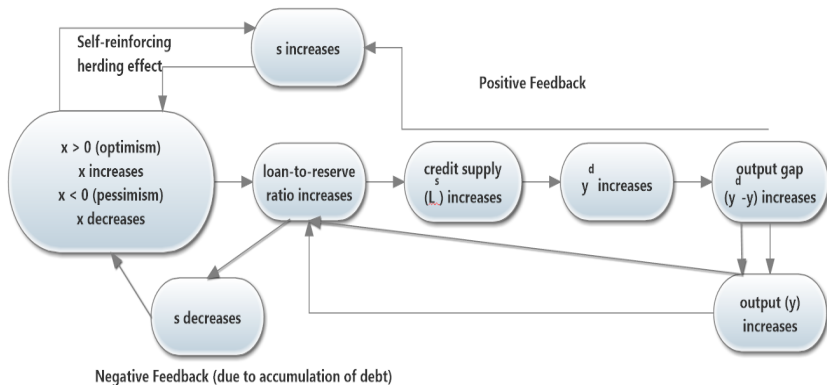


Figure 2: The feedback loop

## The local stability condition

- By setting LHS = 0, we derive the equilibrium of the system:  
 $(\lambda_+^*, y^*, x^*) = (d/(-a_2), y_0^d + k(T_c/2)d/(-a_2), 0)$ .
- The Trace (Tr) and Determinant (Det) of the Jacobian at equilibrium are derived as:

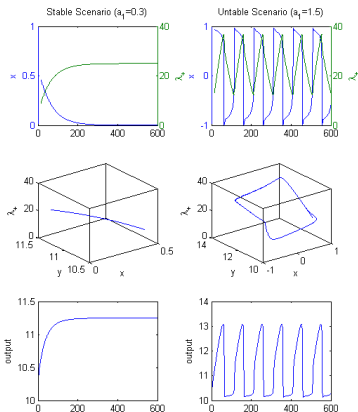
$$Tr = \gamma_2 \sigma k T_c / 2 - \sigma + 2(a_1 + a_3 k(T_c/2))(d/(-a_2) - 1), \quad (18)$$

$$Det = a \sigma \gamma_1 (a_2 + a_3 k T_c / 2) - 2 a_3 \gamma_1 \sigma k T_c / 2. \quad (19)$$

- According to the Routh-Hurwitz condition, two of the necessary (yet not sufficient) conditions for the stability of system (16-18) are:
  - $Tr(J) < 0$  and  $Det(J) < 0$ . In order to satisfy these two conditions we need to have sufficiently small  $a_1$  and  $a_3$ , as well as sufficiently large  $-a_2$ .



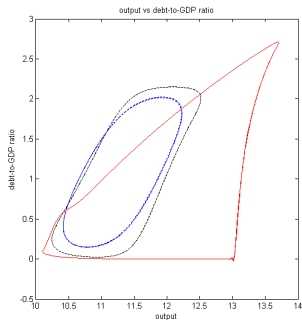
# A Representative Numerical Simulation



**Figure 3:** A Representative Numerical Simulation:  $a_1 = 0.3$  (stable scenario) and  $1.5$  (unstable scenario),  $a_2 = -0.02$ ,  $a_3 = 1.3$ ,  $\sigma = 0.8$ ,  $k = 0.1$ ,  $T_c = 1$ ,  $y_0^d = 10$ ,  $d = 0.5$ ,  $v = 0.4$ ,  $\gamma_1 = 0.5$ ,  $\gamma_2 = 2$

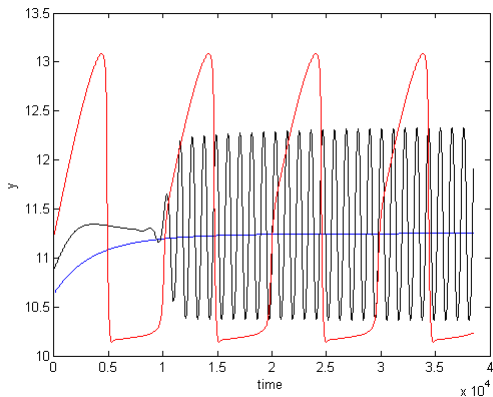
# The Dynamics of the Debt/GDP Ratio

$$\text{Debt/GDP ratio} = L^s / y \quad (20)$$



**Figure 4:** The dynamics of Debt/GDP ratio:  $a_1 = 0.6$  (blue),  $a_1 = 1.1$  (black),  $a_1 = 1.7$  (red)

# Sensitivity Analysis



**Figure 5:** The effect of congestion on output:  $a_1 = 0.3$  (red),  $a_1 = 0.7$  (blue),  $a_1 = 1.5$  (black)

# Sensitivity Analysis

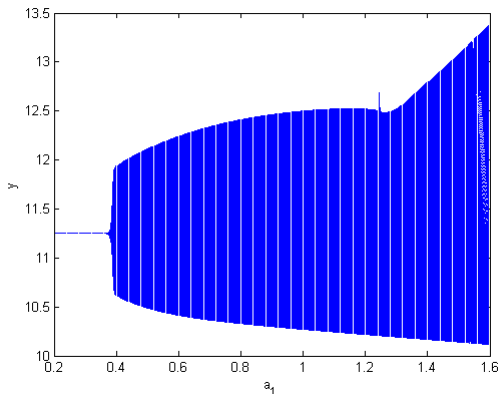


Figure 6: Bifurcation Diagram for  $a_1$

# Sensitivity Analysis

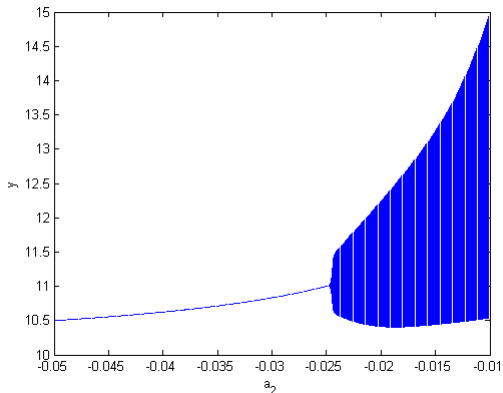


Figure 7: Bifurcation Diagram for  $a_2$

# Sensitivity Analysis

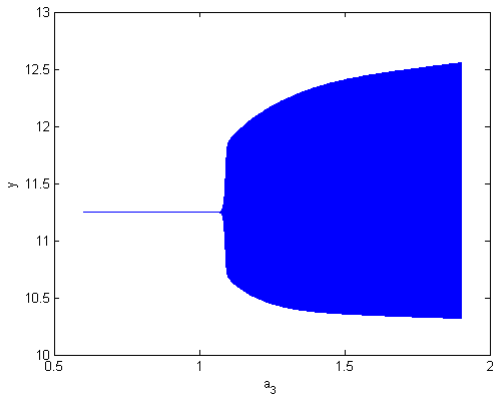


Figure 8: Bifurcation Diagram for  $a_3$

# Sensitivity Analysis

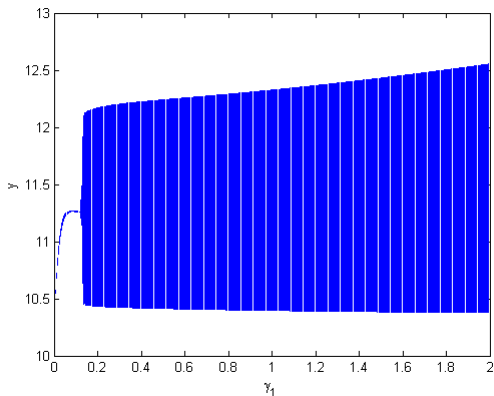


Figure 9: Bifurcation Diagram for  $\gamma_1$

# Sensitivity Analysis

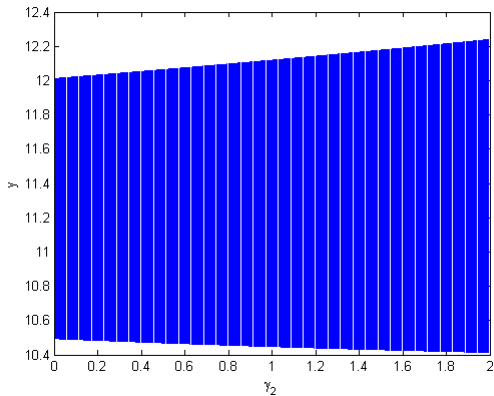


Figure 10: Bifurcation Diagram for  $\gamma_2$



- Introducing Heterogeneous Lending Strategies

$$\dot{\lambda}_+ = \gamma_1(x + g(\cdot)) + \gamma_2\dot{y} + \gamma_3(\bar{\lambda}_+ - \lambda_+), \quad (21)$$

$$\dot{\lambda}_- = \gamma_1(x - g(\cdot)) + \gamma_2\dot{y} + \gamma_3(\bar{\lambda}_- - \lambda_-), \quad (22)$$

$$\dot{y} = \sigma(y^d - y), \quad (23)$$

$$\dot{x} = v[(1 - x)\exp(s) - (1 + x)\exp(-s)]. \quad (24)$$

- Here

$$y^d = y_0^d + kL^s = y_0^d + k(T_c/2)[(1 + x)\lambda_+ + (1 - x)\lambda_-], \quad (25)$$

$$g(\cdot) = \xi_0 \exp(-\xi_1 x^2), \quad (26)$$

$$s = a_1 x + a_{2+} \lambda_+ + a_{2-} \lambda_- + a_3 (y^d - y) + d. \quad (27)$$

## Steady State and Local Stability Analysis

- By setting the  $LHS = 0$ , we derive that
 
$$a_{2+} \left[ \frac{\gamma_1}{\gamma_3} (x + \xi_0 e^{-\xi_1 x^2}) + \bar{\lambda}_+ \right] + a_{2-} \left[ \frac{\gamma_1}{\gamma_3} (x - \xi_0 e^{-\xi_1 x^2}) + \bar{\lambda}_- \right] = \frac{1}{2} \ln \left[ \frac{1+x}{1-x} e^{-2(a_1 x + d)} \right].$$
  - Apparently this equation has no closed form solution.
- Therefore, we consider a special case where the average opinion is neutral at equilibrium ( $x^* = 0$ ).
- The steady state of the system in this special case is given by

$$\lambda_+^* = \bar{\lambda}_+ + \frac{\gamma_1}{\gamma_3} \xi_0, \quad (28)$$

$$\lambda_-^* = \bar{\lambda}_- - \frac{\gamma_1}{\gamma_3} \xi_0, \quad (29)$$

$$y^* = y^{d*} = y_0^d + k(T_c/2)[(\lambda_+^* + \lambda_-^*)], \quad (30)$$

$$x^* = 0. \quad (31)$$

## Steady State and Local Stability Analysis

- To simplify, we exclude the real sector by setting  $\gamma_2 = 0$ ,  $\sigma = 0$ , and  $a_3 = 0$ .
- The Jacobian of sub-dynamics without the real sector is derived as

$$\begin{pmatrix} -\gamma_3 & 0 & \gamma_1 \\ 0 & -\gamma_3 & \gamma_1 \\ 2va_{2+} & 2va_{2-} & 2v(a_1 - 1) \end{pmatrix}.$$

- The trace ( $Tr(J)$ ), determinant ( $Det(J)$ ), and the three principle minors ( $J_i$ ) are derived as follows <sup>2</sup>:

$$Tr(J) = 2[v(a_1 - 1) - \gamma_3], \quad (32)$$

$$Det(J) = 2v[\gamma_3^2(a_1 - 1) - \gamma_1\gamma_3(-a_{2+} - a_{2-})], \quad (33)$$

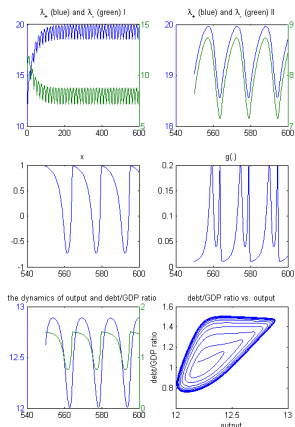
$$J_1 = -2v[\gamma_3(a_1 - 1) + \gamma_1 a_{2-}], \quad (34)$$

$$J_2 = -2v[\gamma_3(a_1 - 1) + \gamma_1 a_{2+}], \quad (35)$$

$$J_3 = \gamma_3^2. \quad (36)$$

<sup>2</sup>According to the Routh-Hurwitz theorem, the necessary and sufficient condition for the stability of the 3D sub-dynamics is that  $tr(J) < 0$ ,  $J_1 + J_2 + J_3 > 0$ ,  $det(J) < 0$ , and  $-tr(J)(J_1 + J_2 + J_3) + det(J) > 0$  (Chiarella and Flaschel 2000).

# Representative Simulation



**Figure 11:** Introducing Heterogeneous Lending Strategies:  $a_1 = 1.5$ ,  $a_{2+} = -0.3$ ,  $a_{2-} = -0.5$ ,  $a_3 = 1.3$ ,  $\sigma = 0.8$ ,  $k = 0.1$ ,  $T_c = 1$ ,  $y_0^d = 11$ ,  $d = 10$ ,  $v = 0.4$ ,  $\gamma_1 = 0.3$ ,  $\gamma_2 = 0.4$ ,  $\xi_0 = 0.2$ ,  $\xi_1 = 3$

# Sensitivity Analysis

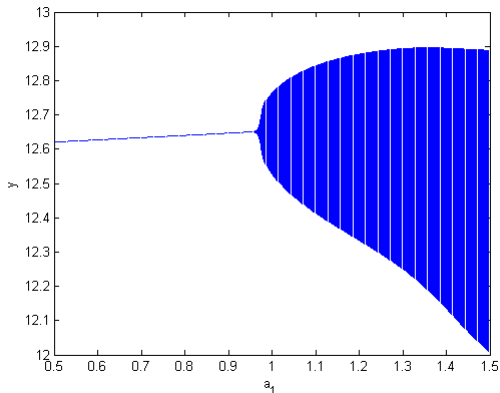


Figure 12: Bifurcation Diagram for  $a_1$

# Sensitivity Analysis

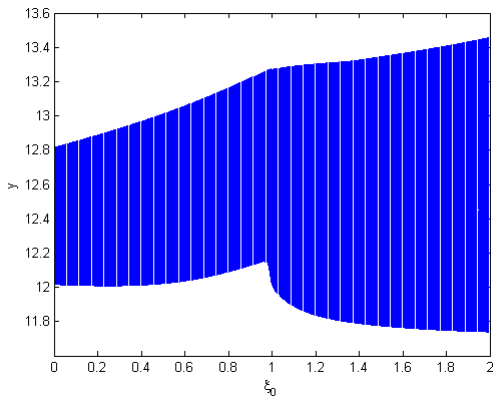


Figure 13: Bifurcation Diagram for  $\xi_0$

# Sensitivity Analysis

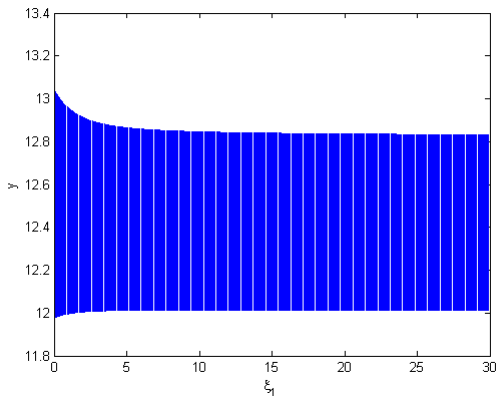


Figure 14: Bifurcation Diagram for  $\xi_1$

## Conclusion






- This paper provides a simple model that aims to examine how the contagious waves of optimism and pessimism contributes to the boom-bust of the credit cycle.
  - It emphasises on the importance of bank’s balance sheet position and its role in credit creation.
- The result is still preliminary, yet it reveals the crucial role of bank’s herding behaviour in creating boom-bust cycle and destabilizing the real economy.



## Limitations

- For the sake of parsimony, our assumption about bankers behaviour is simple.
- We have yet to take into account other important variables such as interest rate and asset price.
- Third, we need a more detailed picture of the macroeconomy that incorporates inflation, unemployment, and so on.
- This can be done by incorporating our model into the recently emerging DSGD-type model developed by Charpe et al (2012).
- The loan-to-reserve ratio takes into account of the *unborrowed* reserves only.
- It is possible to extend the model by incorporating an interbank market, where banks can lend and borrow reserves to each other.

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