

# *Development and testing of an artificial stock market*

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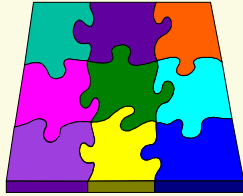
DIEE, University of Cagliari

Silvano Cincotti, Marco Raberto

DIBE, Università di Genova

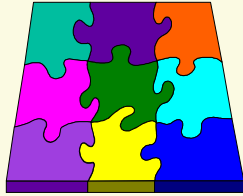
Sergio Focardi

The Intertek Group



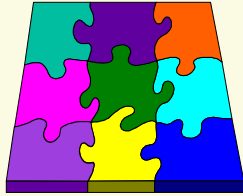
# Summary of the Talk

- ⇒ Introduction
- ⇒ The Genoa Artificial Stock Market (GASM)
- ⇒ GASM microstructure
- ⇒ The market maker
- ⇒ Clustering of traders
- ⇒ System development techniques
- ⇒ Some results
- ⇒ Concluding remarks



# Introduction

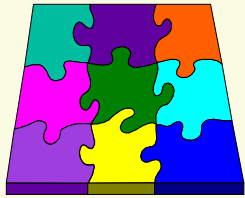
- ⇒ Modern digital computers are so powerful that they allow not only to study reality, but also to simulate it
- ⇒ The availability of a realistic financial market simulator could be very useful for research and practical purposes:
  - ❖ What-if analysis
  - ❖ Financial training and gaming
  - ❖ Volatility studies
  - ❖ ...



# Introduction

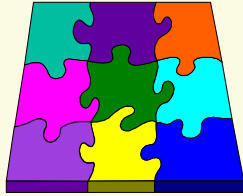
II

- ⇒ Presently, there are some computer simulated financial markets
- ⇒ The most famous is perhaps Santa Fe artificial stock market
- ⇒ Among others, there are:
  - ❖ Vienna University of Economics
  - ❖ MIT
  - ❖ Iowa State University
  - ❖ Max-Planck-Institut, Dresden
  - ❖ ...



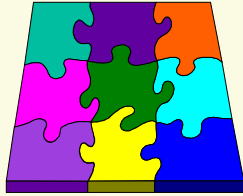
# Yet Another Artificial Stock Market?

- ⇒ We decided to launch a project to build an artificial stock market
- ⇒ We took advantage of the following experiences:
  - ❖ Experience in stock market simulations
  - ❖ Experience in Neural Networks and GA
  - ❖ Experience in software development processes
  - ❖ Experience in Smalltalk language



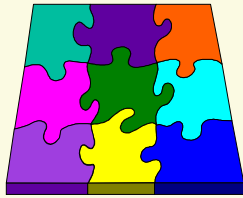
# The Genoa Artificial Stock Market

- ⇒ We called the project “Genoa Artificial Stock Market” (GASM) since:
- ❖ The project is performed mainly at Genoa University, Centre for Economic and Financial Engineering
  - ❖ Genoa was a major financial center in the Middle Ages, where they invented:
    - The I Owe You
    - The first derivative contracts
    - The compound interest



# Main features of GASM

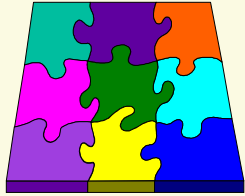
- ⇒ Developed using state-of-the-art programming techniques
- ⇒ Easily upgradable and modifiable
- ⇒ It keeps track of portfolio and cash of every simulated trader
- ⇒ It keeps track of every order and transaction
- ⇒ It is endowed with a realistic price formation mechanism.



# The Genoa market microstructure

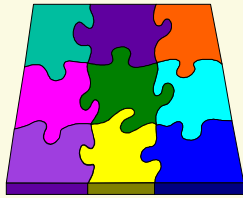
- ⇒ Each trader is an autonomous agent
- ⇒ Traders are endowed with cash and stocks
- ⇒ Traders can issue buy and sell orders
- ⇒ Every trader is tracked by the system
- ⇒ Traders place orders at random
- ⇒ The system has three state variables:
  - ❖ the total amount of cash,
  - ❖ the total number of stocks
  - ❖ the price of the stock





# Genoa market simulation

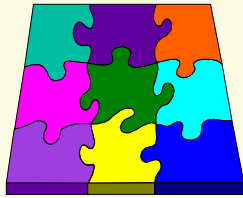
- ⇒ The price computation proceeds in unit time steps of one day
- ⇒ Only one stock is traded in the market
- ⇒ At the beginning of the simulation, the price  $p(0)$  is set in an exogenous way
- ⇒ The price is cleared by a market maker
- ⇒ Once the price is cleared, the compatible orders are executed
- ⇒ Other orders are discarded



# Order generation

- ⇒ At each simulation step, each trader randomly “decides” if and how to trade
- ⇒ First, an extraction is made to decide how many trading operations he/she will perform
- ⇒ Then, for each operation it is decided if it is a buy ( $p = p_b$ ) or a sell ( $p = 1 - p_b$ )
- ⇒ Another random number,  $r$ , is then generated to decide the percentage of cash/stocks to use:

$$\textit{percentage} = 0.9 r \textit{qty}$$



# Order generation

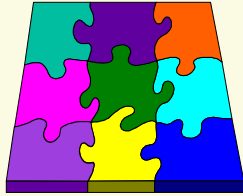
- ⇒ Each buy order has a maximum price, generated at random:

$$p_{max} = p(k) N(1.1, 0.01)$$

- ⇒ Each sell order has a minimum price:

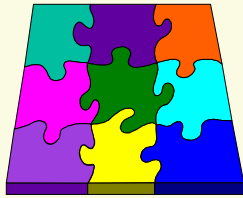
$$p_{min} = p(k) / N(1.1, 0.01)$$

- ⇒ Each order is random, but there is an intrinsic mechanisms of reversion to the mean

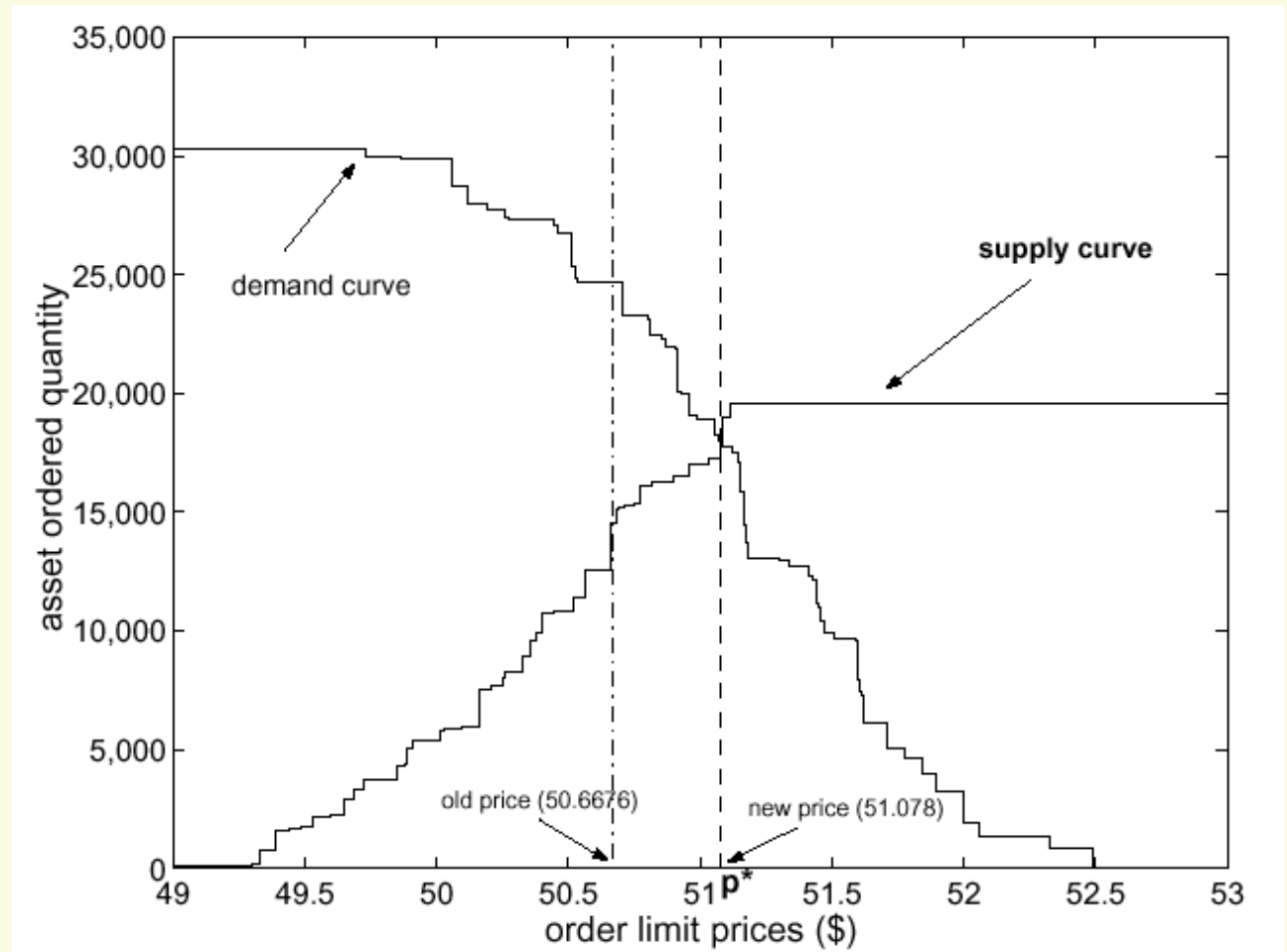


# The market maker

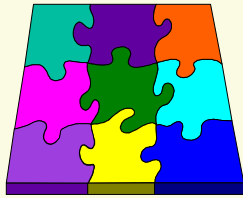
- ⇒ Once orders for time step  $k + 1$  are placed, the market maker determines the optimum price  $p(k + 1)$
- ⇒ Then it clears the market, satisfying all the orders that match this price
- ⇒ The demand and supply curves are computed
- ⇒ Their intersection is the optimum price



# Demand and supply curves

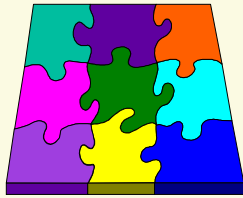


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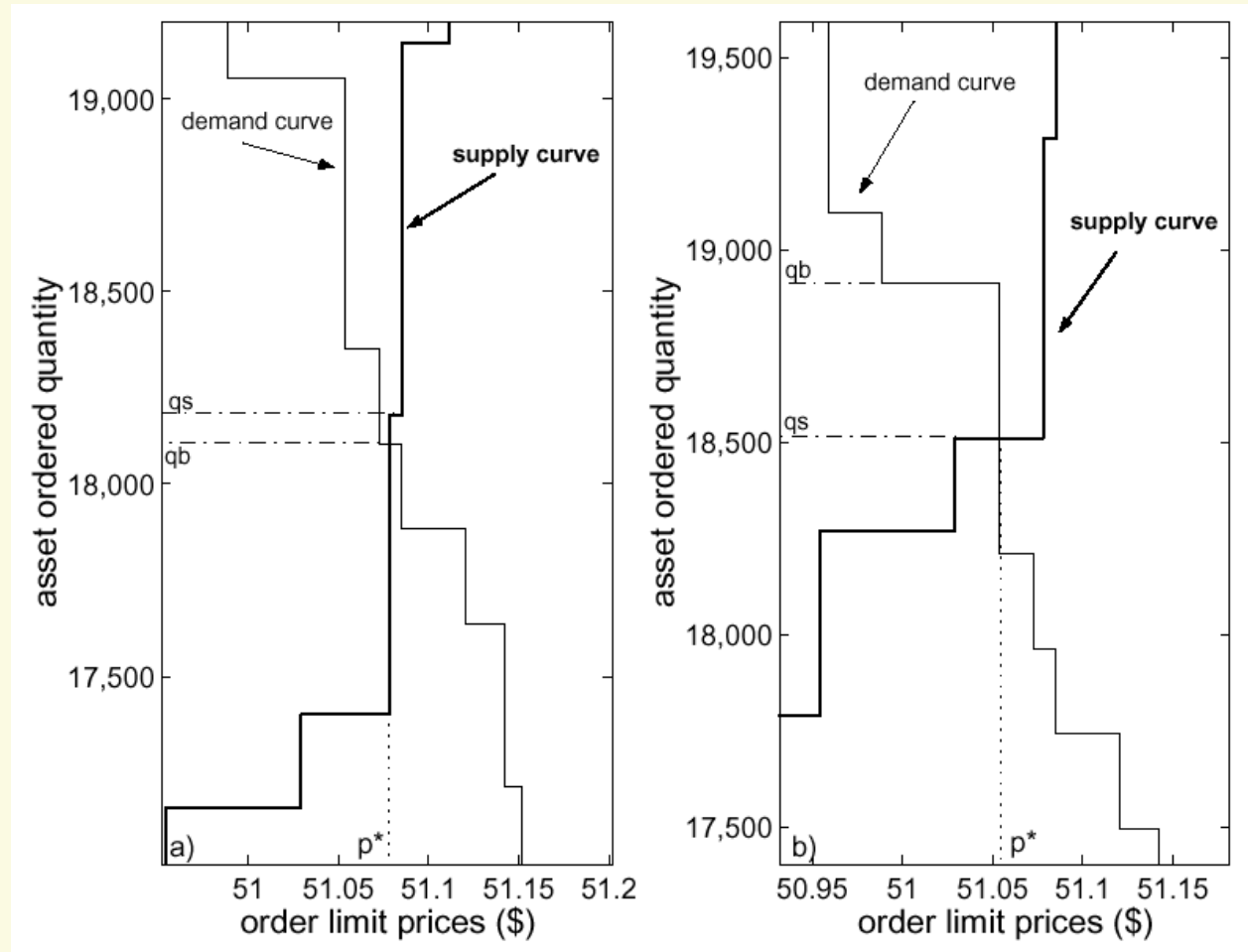


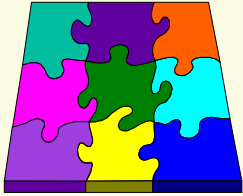
# The market maker

- ⇒ If the size of compatible sell orders is larger than the size of compatible buy orders, the market maker adds cash to the system and subtracts assets from it, and vice-versa
- ⇒ So, we assume an ideal market maker with an unlimited availability of cash and stocks, satisfying all compatible orders
- ⇒ The orders that do not match the clearing price are discarded

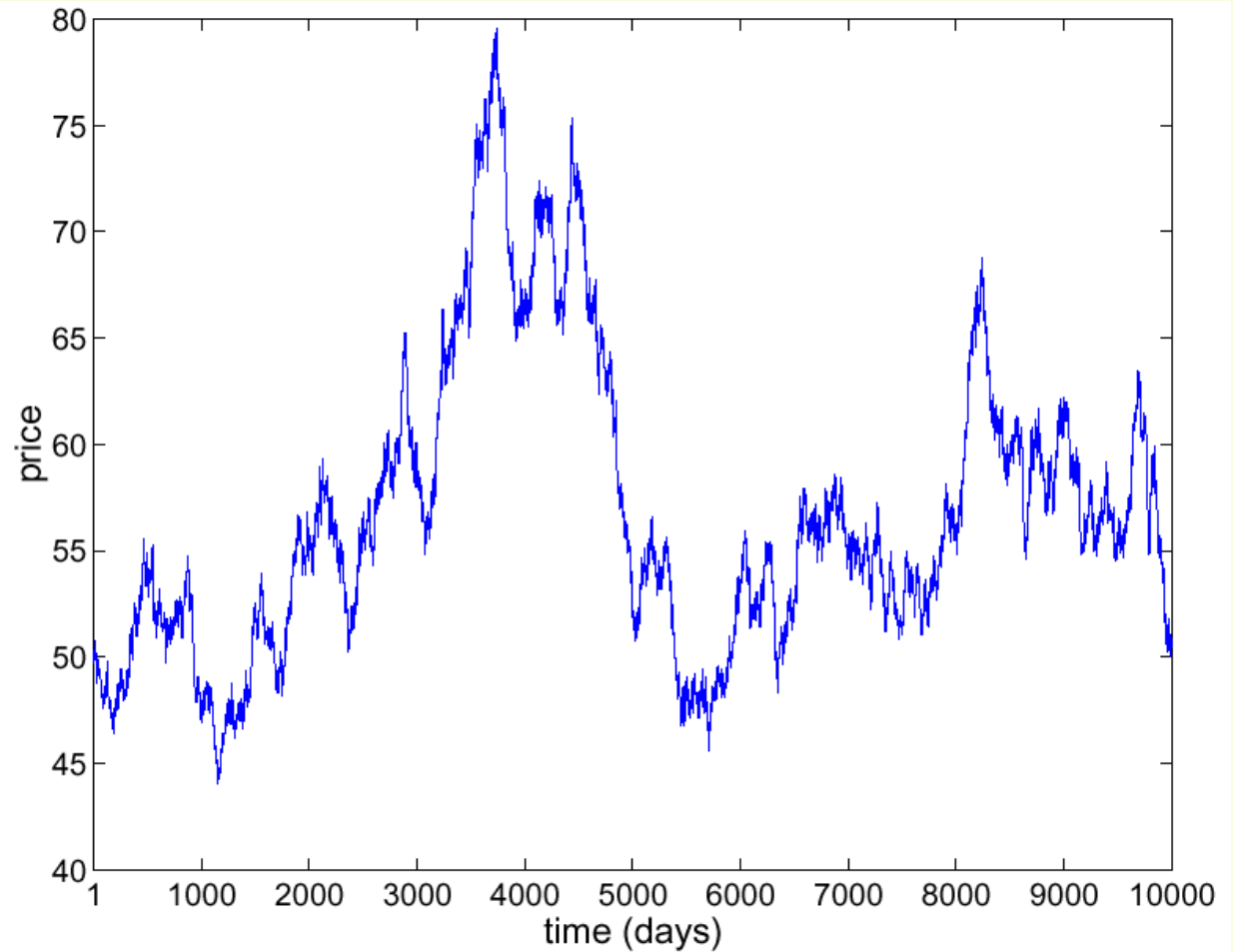


# Demand and supply curves (enlarged view)



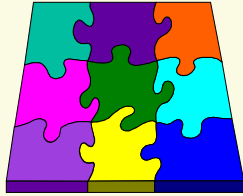


# A price path ( $N = 200$ )

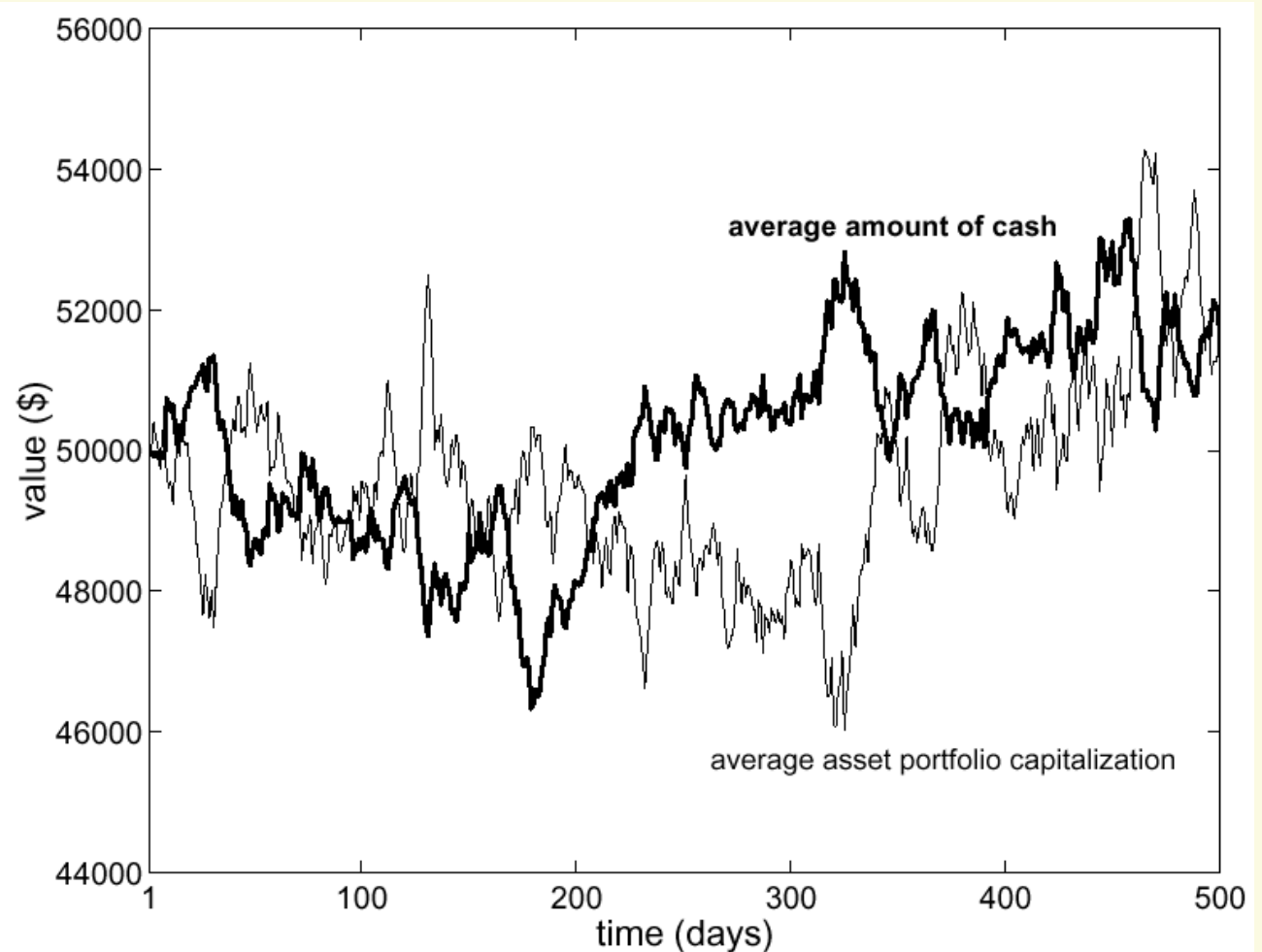


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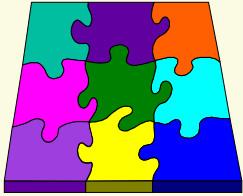




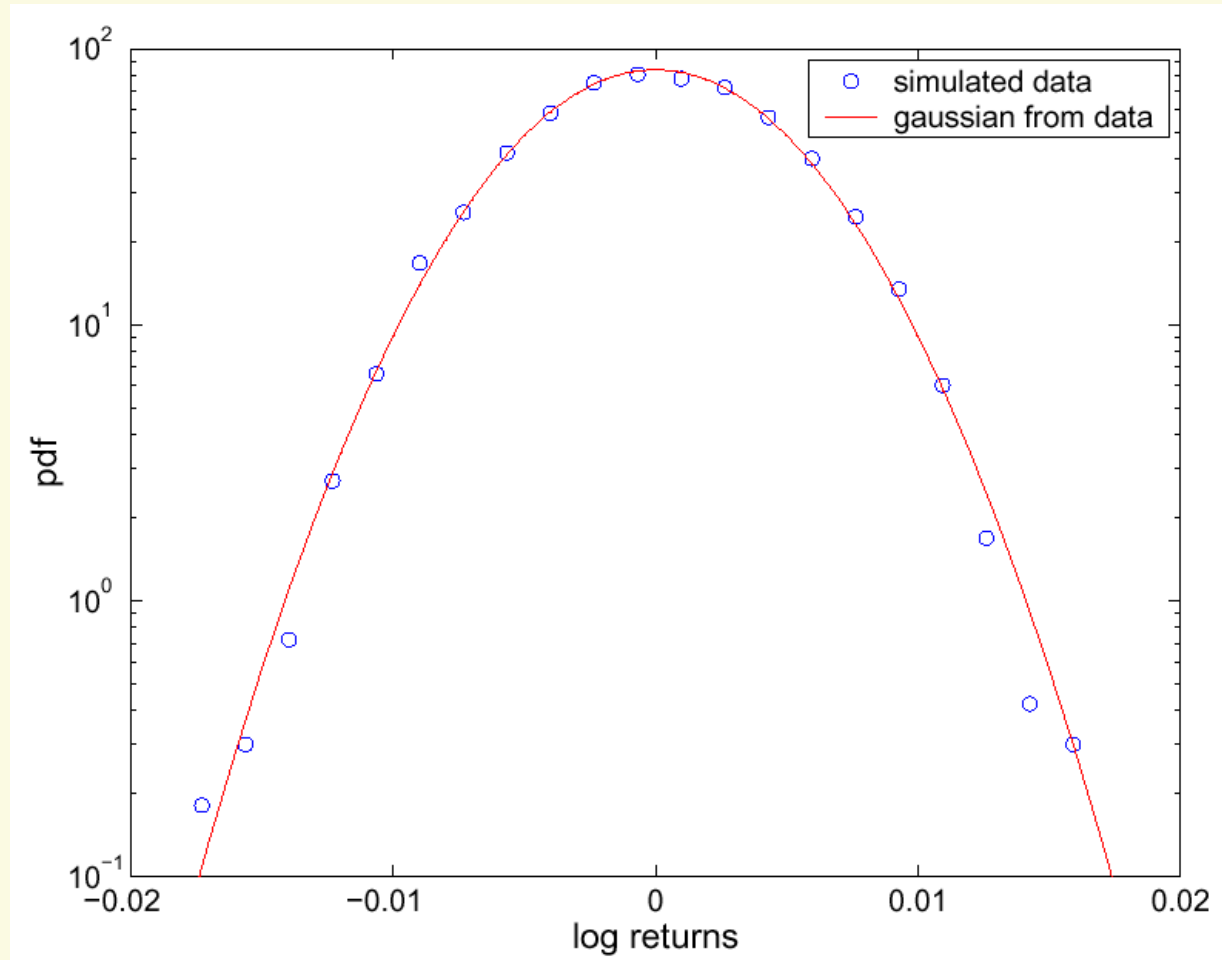
# Cash v/s portfolio capitalization



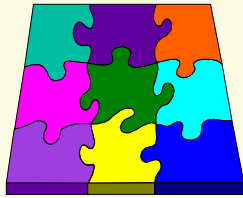
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# Distribution of returns

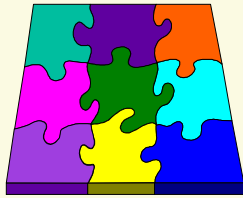


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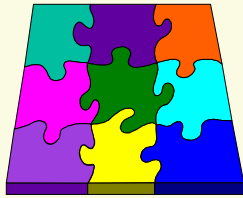
# An aggregation mechanism

- ⇒ The described traders have a balanced behavior and are totally independent
- ⇒ So, it should not be a surprise discovering that daily returns follow a normal distribution
- ⇒ To model the aggregate behavior of traders in real markets we added an aggregation mechanism based on random graphs



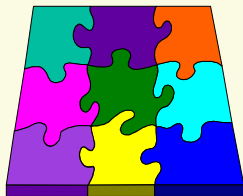
## An aggregation mechanism

- ⇒ Each trader is marked with a *tendency* to be optimist or pessimist (50%-50% at the beginning)
- ⇒ The tendency does not immediately affect the trader behavior
- ⇒ At each time step random links are added with probability  $p_a$  among traders with the same tendency
- ⇒ In this way, clusters of traders sharing the same opinion gradually take shape

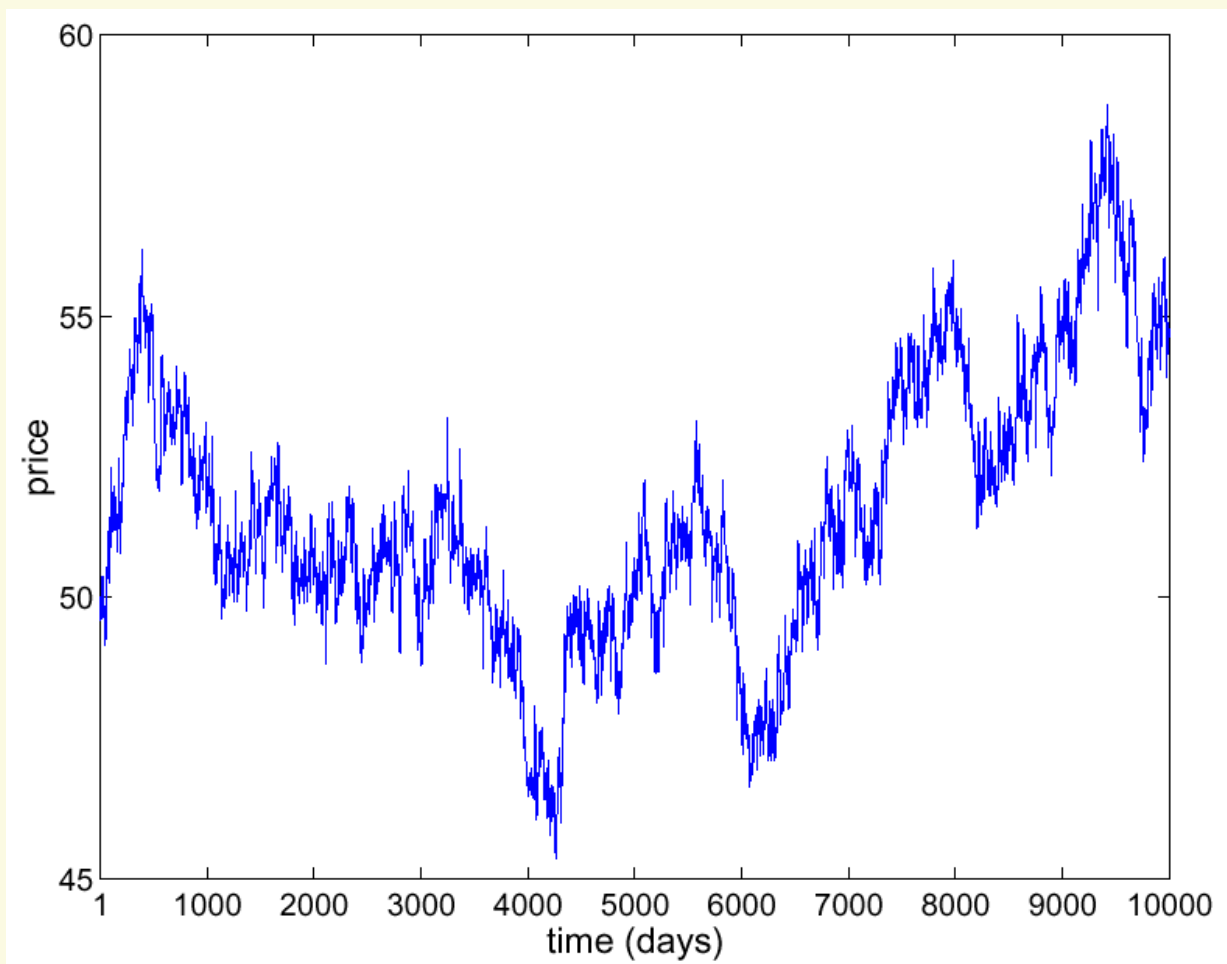


# An aggregation mechanism

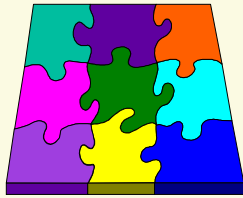
- ⇒ At each simulation step, clusters of both optimist and pessimist traders are randomly chosen with probability  $p_c$
- ⇒ All traders belonging to a chosen cluster receive a message to buy (if optimist) or to sell (if pessimist) as far as they can
- ⇒ Then, chosen clusters are broken and their traders switch tendency
- ⇒ This simplified mechanism mimics opinion formation in real markets



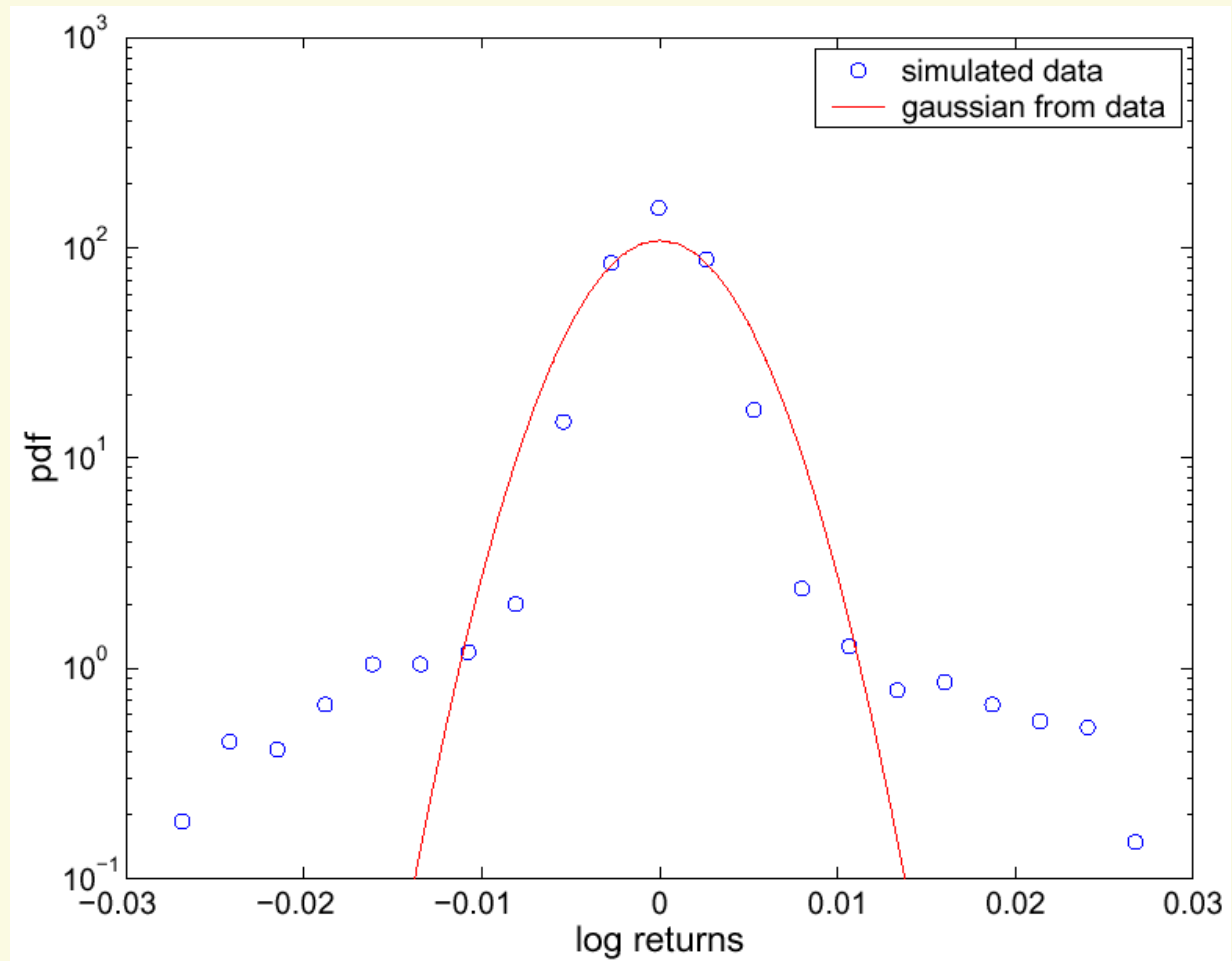
# A price path ( $N = 500$ )



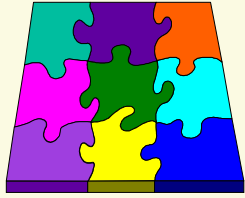
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# Distribution of returns



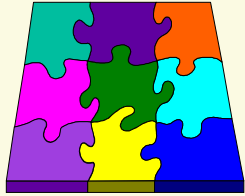
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# Developing market simulation software

- ⇒ The simulator was implemented in Smalltalk
- ⇒ We used pure object-oriented technology
- ⇒ We used eXtreme Programming (XP) as development process
- ⇒ XP is characterized by very short development cycles (1-3 weeks) and thorough automatic testing
- ⇒ Refactoring and simplicity are key concepts in XP





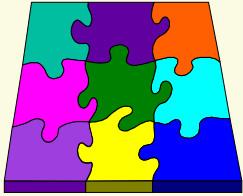
# OO Model of GASM

⇒ 5 subsystems:

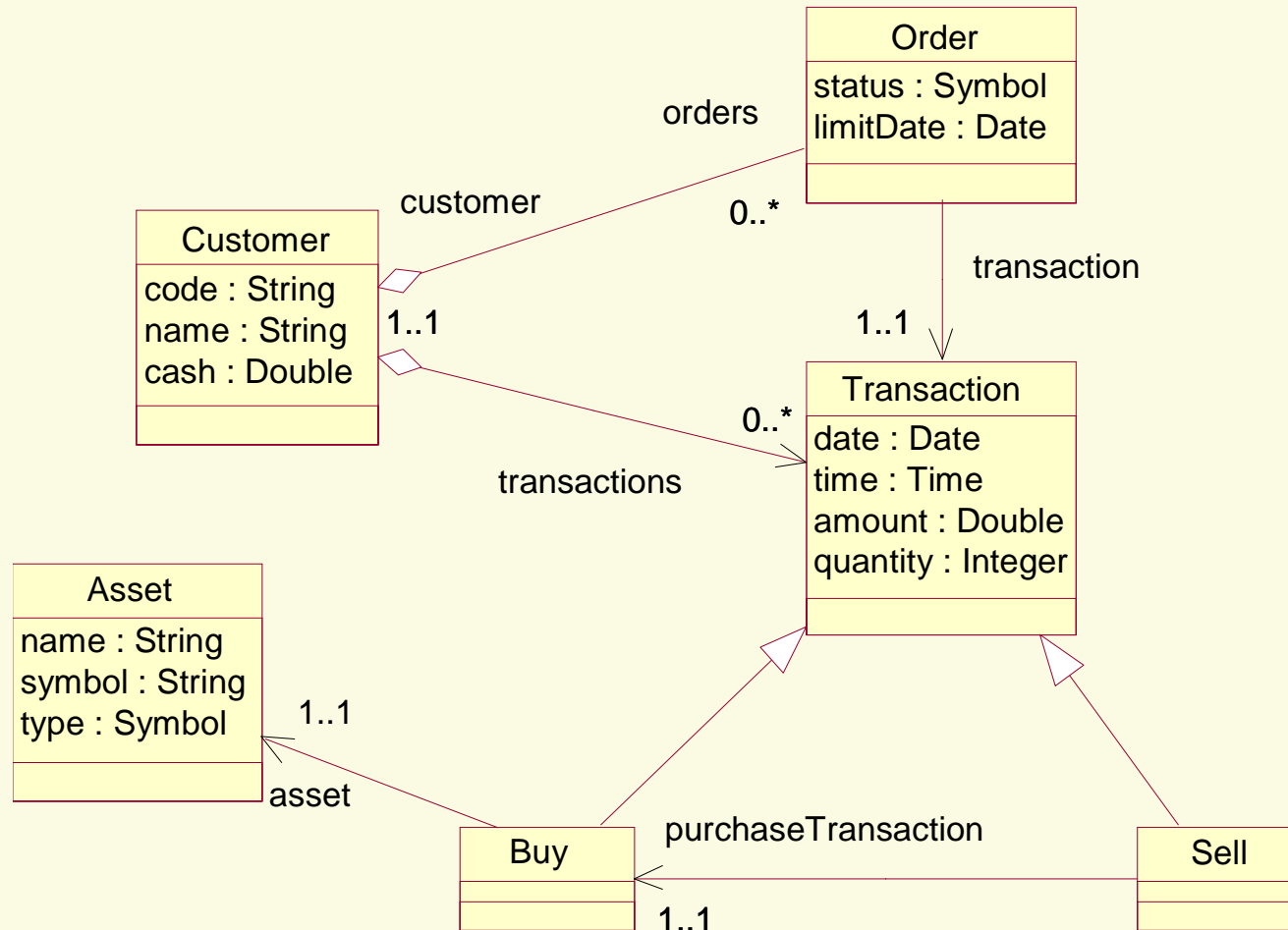
- ❖ Assets
- ❖ Trading
- ❖ Clusters
- ❖ Simulation
- ❖ Testing

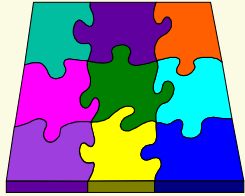
⇒ System documentation in UML

⇒ System conceived to grow and to be easily modified



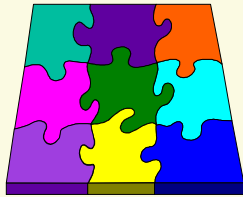
# An UML class diagram



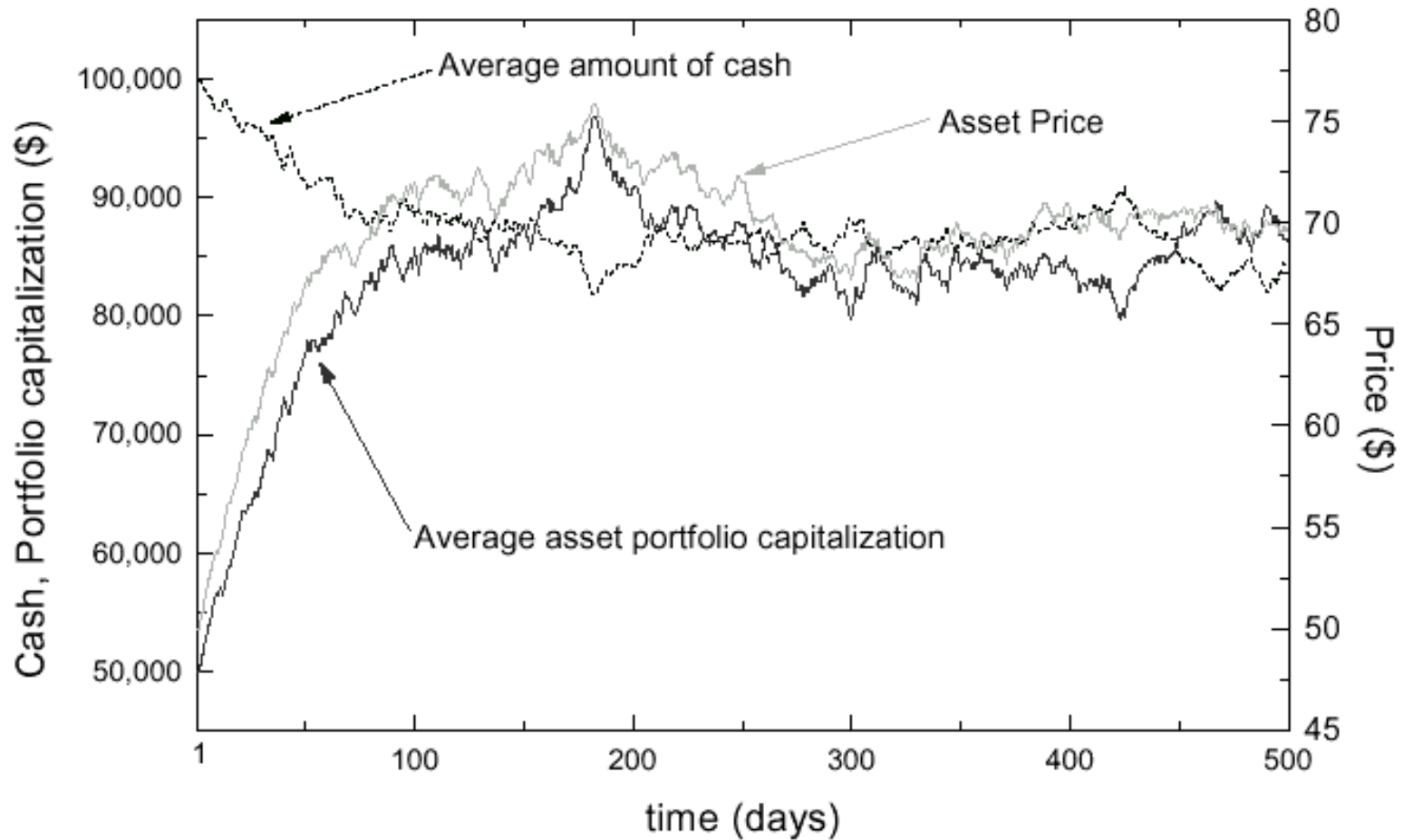


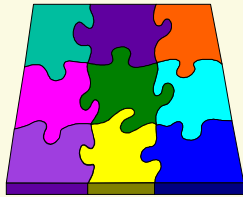
## Some actual figures

- ⇒ Present system: 18 classes and 220 methods
- ⇒ Test suite of 11 classes and 112 methods
- ⇒ 100 traders for 1000 time steps can be simulated in about 4' on a Pentium III 600MHz computer
- ⇒ A first release of GASM was operational in 3 months

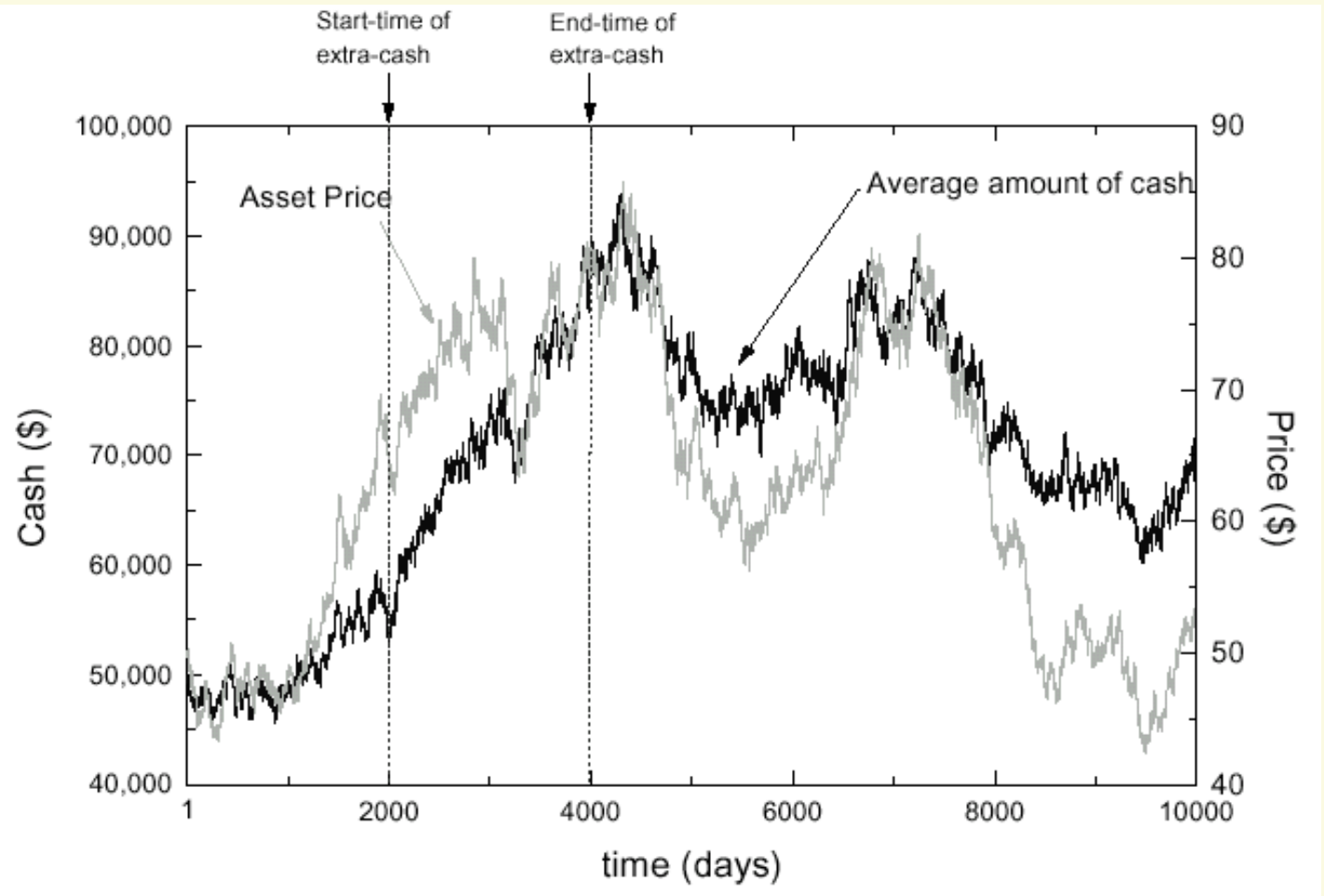


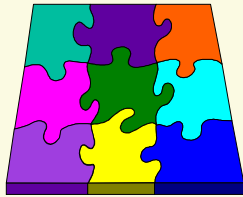
# A simulation example





# Another example





# Concluding Remarks

- ⇒ The system is operational and used for research experiments
- ⇒ GASM has been conceived to continuously evolve
- ⇒ Present projects:
  - ❖ Add intelligence to traders (with NN and GA)
  - ❖ Link the artificial stock with a simulated “economy”
  - ❖ Build a trading game on GASM, in which players’ operations may influence the market